

TOP DOWN PARSERS

Parses an input string starting from start symbol and through a series of derivations reaches out to string (if it can be parsed)

Recursive-Descent Parsing - is a form of top-down parsing that may require backtracking

- Consists of a set of procedures, one for each nonterminal

PREDICTIVE PARSER - Special case of recursive-descent parsing that does not require backtracking

- Lookahead symbol unambiguously determines which production rule to use
- Advantage is that the algorithm is simple and the parser can be constructed by hand

Requirement of Grammar (Top Down Predictive Parser)

LL(1) Grammars - A grammars free from Left recursion and backtracking, Thus does not cause duplicate entries into parsing table

First L stands for left-to-right scan, second L stands for leftmost derivation

- There is one lookahead token
- In LL(k), k stands for k lookahead tokens
- Predictive parsers accept LL(k) grammars

Two major problems of top down parser

1. Backtracking
2. Left recursion

Any CFG grammar is not suitable to be used for Top-down parser. If problems as stated above persists in the CFG, It should be removed first. The resultant grammar is called LL(1).

Parsing Table Construction

It requires computations of **FIRST AND FOLLOW SETS**

FIRST Set

1. If X is a terminal, then $\text{FIRST } X = \{X\}$
2. If $X \rightarrow \epsilon$ is a production, then $\epsilon \in \text{FIRST}(X)$
3. If X is a nonterminal and $X \rightarrow Y_1 Y_2 \dots Y_k$ is a production then,
 - I. Everything in $\text{FIRST}(Y_1)$ is in $\text{FIRST } X$
 - II. If for some i , $a \in \text{FIRST}(Y_i)$ and $\forall 1 \leq j < i, \epsilon \in \text{FIRST}(Y_j)$, then $a \in \text{FIRST}(X)$
 - III. If $\epsilon \in \text{FIRST}(Y_1 \dots Y_k)$, then $\epsilon \in \text{FIRST}(X)$

FOLLOW Set

Defined as the set of terminals that can immediately follow X , that is, $t \in \text{FOLLOW}(X)$, if there is any derivation containing Xt

1. $\$$ is in $\text{FOLLOW}(S)$ where S is the start symbol and $\$$ is the end marker
2. If there is a production $A \rightarrow \alpha B \beta$, then everything in $\text{FIRST}(\beta)$ except ϵ is in $\text{FOLLOW}(B)$
3. If there is a production $A \rightarrow \alpha B$, or a production $A \rightarrow \alpha B \beta$ where $\text{FIRST}(\beta)$ contains ϵ , then everything in $\text{FOLLOW}(A)$ is in $\text{FOLLOW}(B)$

Predictive Parsing Table Construction Algorithm

Input: Grammar G

Algorithm:

1. For each production $A \rightarrow \alpha$ in G ,
2. For each terminal a in $\text{FIRST } \alpha$, add $A \rightarrow \alpha$ to $M[A, a]$
3. If ϵ is in $\text{FIRST } \alpha$, then for each terminal b in $\text{FOLLOW}(A)$, add $A \rightarrow \alpha$ to $M[A, b]$
4. If ϵ is in $\text{FIRST } \alpha$ and $\$$ is in $\text{FOLLOW}(A)$, add $A \rightarrow \alpha$ to $M[A, \$]$
5. No production in $M[A, a]$ indicates error

Predictive Parsing Algorithm

Input: String w and parsing table M for grammar G

Algorithm: Let a be the first symbol in w

Let X be the symbol at the top of the stack

while $X \neq \$$:

if $X == a$:

Pop the stack and advance the input

else if X is a Non terminal or $M[X, a]$ is an error entry:

error

else if $M[X, a] == X \rightarrow Y_1 Y_2 \dots Y_k$:

output the production

pop the stack

push $Y_k Y_{k-1} \dots Y_1$ onto the stack

$X \leftarrow$ top stack symbol

Example:

$$E \rightarrow E + T \mid T$$
$$T \rightarrow T * F \mid F$$
$$F \rightarrow (E) \mid \text{id}$$

Grammar has left recursion. So after modifications

$$E \rightarrow TE'$$
$$E' \rightarrow +TE' \mid \epsilon$$
$$T \rightarrow FT'$$
$$T' \rightarrow * FT' \mid \epsilon$$
$$F \rightarrow () \mid \text{id}$$

